

eg. A spring is 20.0 cm long. When I hang a 500 g mass on it, it extends to 39.0 cm. I pull the mass down 2.0 cm and let go. Determine:

a) elastic constant

$$\begin{aligned} F &= -kx \quad k = F/x = mg/(L_2 - L_1) \\ &= (0.50 \text{ kg} \times 9.8 \text{ N/kg}) / (0.390 \text{ m} - 0.200 \text{ m}) \\ &4.9 / 0.19 = 25.7895 \\ &= \boxed{25.8 \text{ N/m}} \end{aligned}$$

why 19cm for x? that is equilibrium point, where elastic force = gravitational force

b) elastic energy relative to the equilibrium position when you pull it down 2.0cm.

$$\begin{aligned} E_{\text{elastic}} &= \frac{1}{2} kx^2 = 0.5 \times (25.7895) \times (0.02) \times (0.02) = \\ &\boxed{0.0052 \text{ J}} \end{aligned}$$

c) kinetic energy when it is in the equilibrium position

$$\begin{aligned} E_k &= \text{elastic energy if no energy is lost} \\ &= 0.0052 \text{ J} \end{aligned}$$

d) speed at equilibrium position

$$\begin{aligned} \frac{1}{2}mv^2 &= E_k \\ v &= \sqrt{2 \times 0.0052 / 0.5} = 0.14422205101856 \\ v &= 0.144 \text{ m/s} \end{aligned}$$

$0.242 - 0.167 = 0.075$  peak to trough distance,  
so amplitude =  $0.075/2 = 0.0375$

$$\frac{1}{2} mv^2 = \frac{1}{2} kx^2$$

$$x = \sqrt{m/k} v$$

$$v = \sqrt{k/m} x$$

last question:

sketch the energy graph, showing elastic energy, kinetic energy and total energy of the 0.50 kg mass on the spring,  $k=26\text{N/m}$  with amplitude of 2.0cm. Energy vs x

review kinematics:

eg. A car is moving at 15.0 m/s and slows to 10.0m/s. determine the acceleration if

- a) the change takes 12.0s
- b) the change is over a distance of 30.0 m

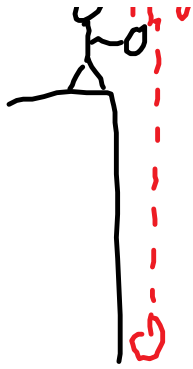
A ball is thrown up off a 30.0 m high cliff with a speed of 8.00m/s.

- a) how high does the ball go?
- b) what is the speed of the ball when it hits the base of the cliff?
- c) how long does it take to hit the base of the cliff?



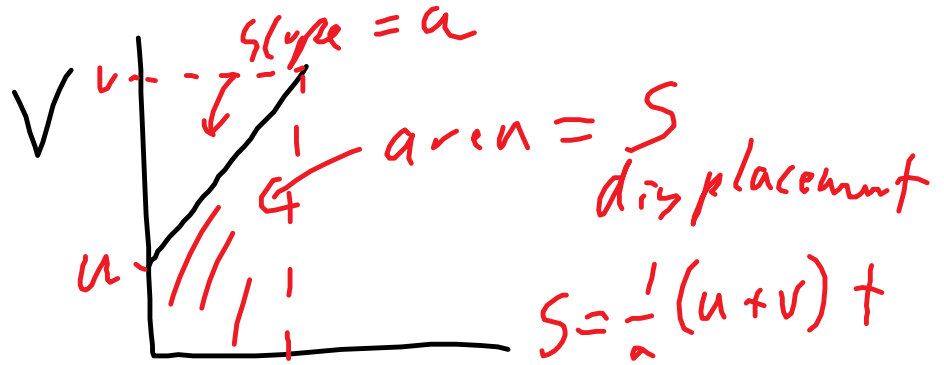
uniform acceleration

$$a = \Delta v / \Delta t = (v_{\text{final}} - v_{\text{initial}}) / t \text{ where } v_{\text{initial}} \text{ is initial}$$



uniform acceleration

$a = \Delta v / \Delta t = (v - u) / t$  where  $u$  is initial velocity ( $a$  is slope of  $v-t$  graph)

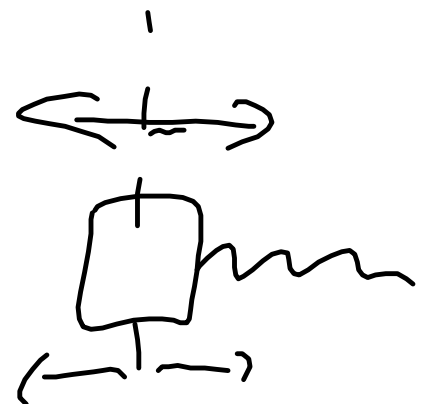
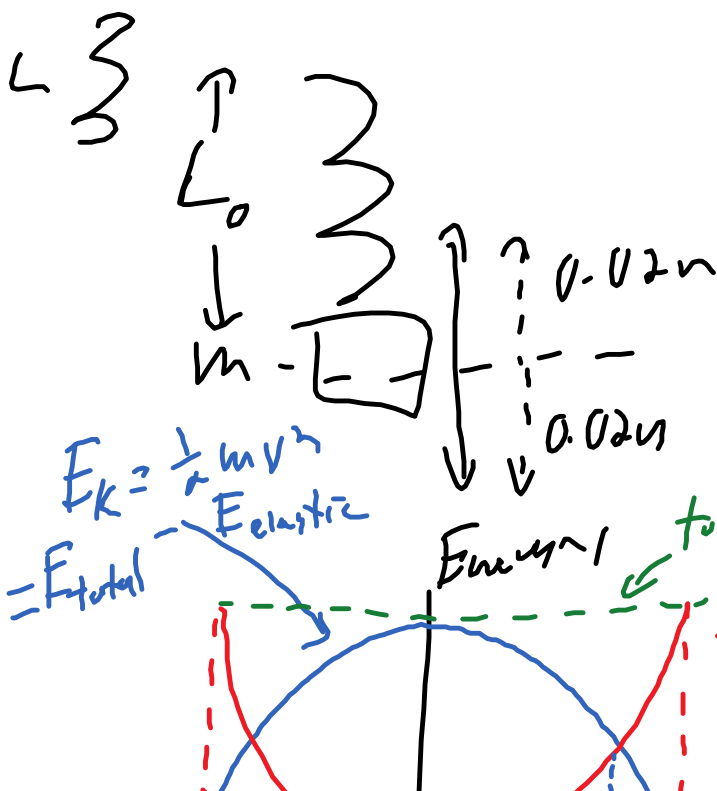


$$V^2 = 2as + u^2$$

$$s = ut + \frac{1}{2} at^2$$

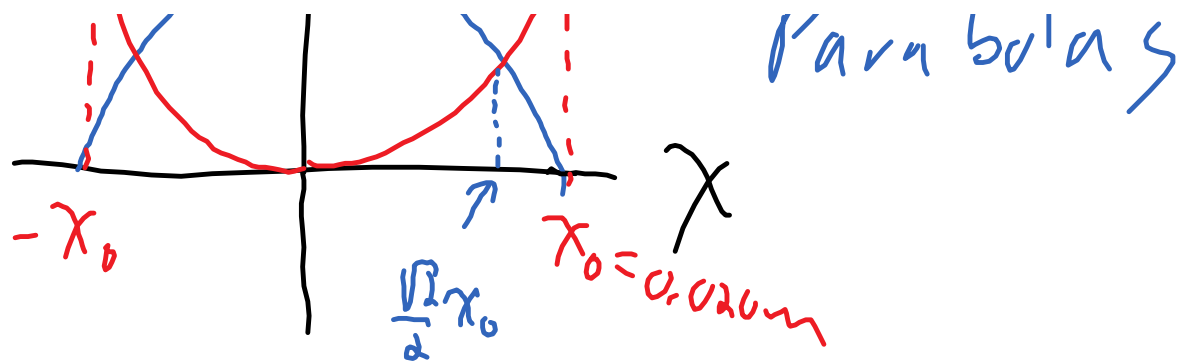
P38-40

Q21, 27, 33, 39, 41, 45



$$E_{elastic} = \frac{1}{2} kx^2$$

Parabolas



$$a) a = \frac{V - u}{t} = \frac{10.0 \text{ m/s} - 15.0 \text{ m/s}}{12.0 \text{ s}} = -0.42 \text{ m/s}^2$$

$$b) d = 30.0 \text{ m}, V = 10.0 \text{ m/s}$$

$$a = ?, u = 15.0 \text{ m/s}$$

$$V^2 = u^2 + 2as$$

$$a = \frac{V^2 - u^2}{2s} = \frac{10^2 - 15^2}{2(30)}$$

$$a = -2.08 \text{ m/s}^2$$